

Graphic Logarithmic Tables¹

A Picture Should Be Worth A Million Numbers²



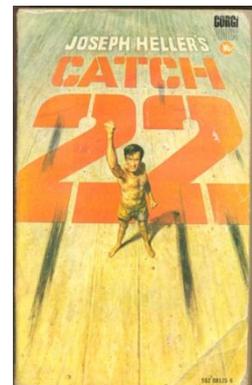
Given what they replaced it feels disparaging, impolite and almost blasphemous to point out that logarithmic tables were sadly error prone and irritatingly awkward to use. Surely graphic logarithmic tables must have been the answer!



It is fitting to remember in 2014, the year of their 400th anniversary, that before John Napier (1550-1617) invented logarithms most forms of computation were complex and enormously time-consuming. In fields like navigation and astronomy it took elite mathematicians of the day³ literally years to finish some calculations. So what on earth could there be about logarithmic tables to complain about?

Catch-22

The work on logarithms undertaken by Napier was a classic Catch-22 style paradox⁴. First he had to work through the tedious calculations needed to create all the entries in a set of logarithmic tables and then find a way to verify them. But the supreme irony is that once the tables existed, they would have made it much easier to do the calculations in the first place! A modern-day Catch-22 analogy would be computer programming. Once a program compiler was developed, programmers no longer had to write programs in machine code. But first someone had to write a compiler in machine code.



Napier, aided by his own “Napier bones”, did set about the enormity of the task with considerable insight and ingenuity. His first challenge was to shake off 16th century mathematical thinking of the time. Before Napier invented logarithmic tables mathematicians of the day relied on fixed sequences. For example, the fixed arithmetic sequence of 0, 1, 2, 3, 4, etc or the fixed geometric sequence of 1, 2, 4, 8, 16, etc. This worked fine when stepping through a series of whole numbers but clearly

¹ Research findings by the author published in 2013 as part of the “*Collectanea de Logarithmis*” DVD.

² Derived from a 20th century phrase coined by American Frederick R. Barnard.

³ In Napier’s day such calculation experts were known as: “Reckoners”.

⁴ The impossible paradox famously introduced in Joseph Heller’s 1953 book of the same name.

overlooked all the values in between. So Napier broke with tradition and decided to adopt a **kinematic approach** for building his tables. This way he would have “no numerical gaps” – i.e. he defined: (i) an arithmetic and continuous movement of a point along a single straight line with a constant speed AND (ii) a proportional and continuous movement of point along a straight line with a proportional speed.

The completeness of his tables was not the only “Catch-22” dilemma Napier had to overcome. He had no precedent for the degree of accuracy the values in his tables needed to have. With this quandary came another conundrum – for a given degree of accuracy, how much work would that involve to generate the full table? So Napier came up with what today would be called a **meta process**. Having developed a means of calculating a series of values, he would then evaluate the values obtained to see how they could be used to generate more values i.e. a meta calculation process.

So by adopting a kinematic approach and a meta process, Napier achieved an insightful balance between the desired degree of accuracy and the tedious longhand calculations needed to generate the table entries.

Gr.	Sinus	Logarithmus	Differentia	Logarithmi	Sinus
0	10000000	81425681	81425680	0	10000000
1	9999999	74424411	74424411	1	10000000
2	9999998	67423141	67423140	2	9999998
3	9999997	60421871	60421870	3	9999997
4	9999996	53420601	53420600	4	9999996
5	9999995	46419331	46419330	5	9999995
6	9999994	39418061	39418060	6	9999994

Part of Napier's “*Mirifici Logarithmorum Canonis Descriptio*”

Published errors

Inevitably a few errors did creep into Napier’s original calculations and indeed into the calculations made by later authors who devised extended versions (e.g. greater number of significant places) or designed new types of logarithmic tables. Some of the earliest errors went unnoticed and were repeated or compounded in some of the tables published much later. But even if it had been humanly possible for Napier to generate and note down all the entries needed for his logarithmic table totally error-free, many mistakes got introduced during the typesetting and printing.

When copying or duplicating a long list of numerals, apart from any other oversights, unintentionally transposing two adjacent numbers is a known human weakness. Then came the thankless task poorly paid typesetters had to face. Typesetting row upon row of seemingly random numerals in a printing block must have been a really mind-numbing task. It was unintentional but understandable how typesetting errors ended up in many logarithmic tables. For example, errors made in the last decimal place were particularly difficult to spot. Such mistakes often remained unnoticed for decades and were perpetuated when inherited from one publishing house to another and logarithmic tables got reissued or republished.

Logarithmic tables can be a pain

Arguably, given the longhand nature of calculating the table entries and then the mind-numbing typesetting needed to publish them, the odd error was a small price to pay for how logarithmic tables made all kinds of multiplication and division much simpler and momentarily quicker to perform. As it turned out, the immeasurable gains that logarithmic tables made possible far outweighed the more obvious tangible benefits. Top of the list of immeasurable gains were:

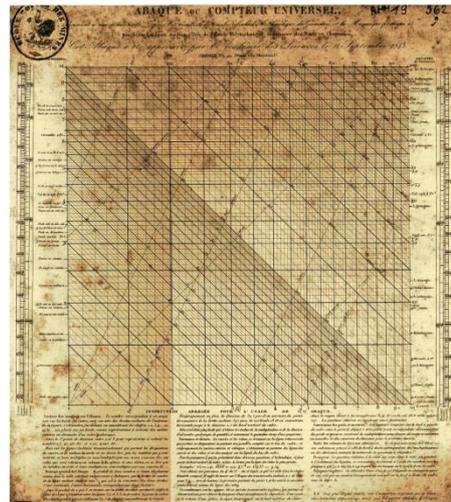
- 1. individuals other than “mathematical geniuses” could now attempt complicated calculations**
- 2. scientists and mathematicians could now (in their lifetimes) unlock and solve many mathematical conundrums which in turn lead to many advancements and discoveries in many different fields**

However, despite being a paradigm shift when compared with the old pre-logarithm ways, the very nature of the concept meant using tables had distinct disadvantages. The ritualistic look-up process could be irritating and so long-winded that without fastidious care, it could itself easily become error-prone. Also some factors commonly found in calculations could make using early logarithmic tables tricky and a real pain to use. For example, negative numbers or answers needing a high degree of accuracy - say significant to at least 7 or 8 significant places. A workaround for negative numbers was to handle the sign separately. Often the drawbacks got magnified many times over when attempting complex calculations. Finally the sheer number of times an interim solution had to be looked up in a logarithmic table became a test of concentration and patience.

So despite the many obvious advantages, logarithmic tables were not error-free and using them was error-prone and irritating. But centuries after logarithmic tables were first published an innovative and elegant solution was found for most of the drawbacks and the tedium - **graphic logarithmic tables**.

Nomograms showed the way

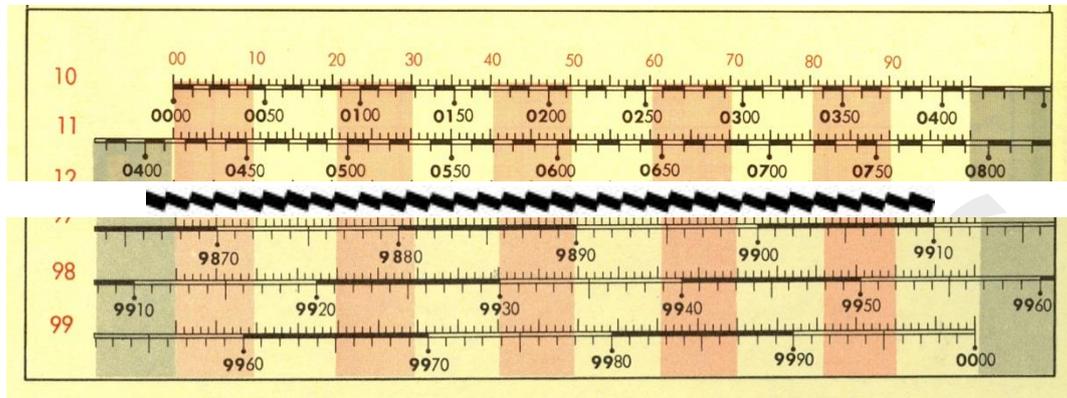
Like many great ideas, the appeal of a nomogram comes from its simplicity. It is a two-dimensional diagram designed to show the approximate “graphic calculation” of a mathematical function. The most basic nomogram having two parallel outer scales representing the values of two quantities involved in a function. Where the lines joining quantities used in the calculation intersect, gives the result of the function. An early advocate of the nomogram was Frenchman *Leon Louis Lalanne* (1812-1892). In 1843, with his “Universal Calculator”, he probably created the first log-log plot.



Sadly some nomograms became so complex that the function(s) they represented were just as difficult to grasp as their inherent longhand mathematical formula. However, it is the same basic idea that a picture is easier to understand than a long list of numbers that led to graphic logarithmic tables being developed.

So what are graphic logarithmic tables?

Printed as a single linear scale (end-to-end scale lengths varying from as little as 4.1m to as much as 115m – see *Appendix A* for the details) they clearly look strikingly different from the many rows and columns of similar looking numerical entries in a traditional logarithmic table.



The beginning and the end of an example graphic logarithmic table

Instead they somewhat reflect the concepts of a calculation aid based on rods and scales Professor Johann Gottfried Steinhäuser theorised about in 1807. A closer match is the intriguing prototype disc for a graphic logarithmic table⁵ proposed by a medical officer in the French Army, Dr Haro, in 1887. Regardless of the inspiration, the differences when compared to traditional logarithmic tables are much more than just an innovative printing or formatting style. In a graphic logarithmic table:

- **all the entries in the log and antilog sections of a traditional logarithmic table have been integrated into a single, much shorter “endless” entry**
- **the look-up process is simpler, quicker and much more intuitive**

But it is also important to set boundaries on what constitutes a graphic logarithmic table as they come in various shapes and sizes and many loosely related “cousins” exist. For example, a slide rule (in its many forms) has logarithmic scales that provide answers without needing to resort to antilogs. However, for practical reasons the logarithmic scales normally found on slide rules only ever represent a subset of all the entries found in any traditional or graphic logarithmic table. By using a subset or leaving out rarely needed parts of the range was one of the few ways slide rule designers could usefully compact the length of a scale and ultimately, the length of the slide rule. Only the largest drum and grid-iron types had enough room for a range of values that got close to the full range of values included in any logarithmic table. Without these boundaries, a plethora of other printed calculating aids and slide charts could arguably have been called types of graphic table.

So unlike slide rules and similar calculating devices, graphic logarithmic tables still rely on a table look-up process and apart from one exception, all known examples exist as some form of printed page or more commonly, a slim book.

⁵ As far as is known the concept was never developed further than the paper Dr Haro submitted to the “*Association Francaise pour L’Avancement des Sciences*” 1887 conference in Toulouse.

Graphic logarithmic tables – how did they work?

The easiest way to show how such graphic logarithmic tables were used is a worked example. However, the developers of such tables chose an eclectic variety of ways to achieve the same goal. Despite these design differences, the way they were used, when compared with a traditional logarithmic table, is universal.

The chosen example, 2.5×5 , looks trivial but enough to show the generic process. The only drawback is that the simplicity of the example hides the full tedium of and error-prone nature of the repetitive look-up process when using traditional logarithmic tables for complex calculations. Conversely the advantages of a graphic logarithmic table are amplified many times over for such complex calculations.

Using a traditional table of logarithms

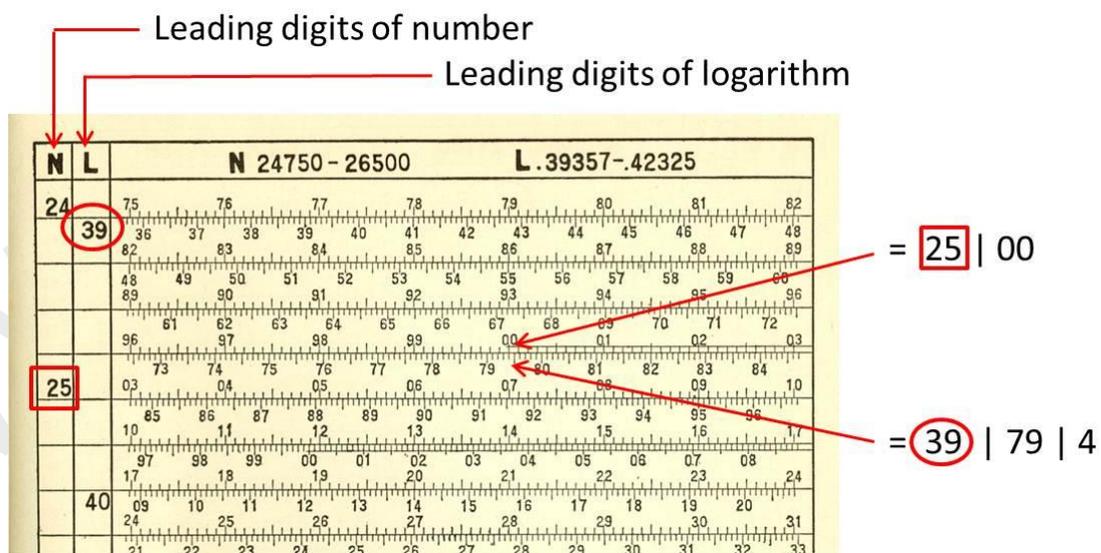
With a table compiled for 5 decimal places⁶ the minimum calculation steps are:

	=
1. Look-up the logarithm of 2.5	0.39794
2. Look-up the logarithm of 5	0.69897
3. Add the Log of 5 to the Log of 2.5	1.09691
4. Look-up the antilog of the mantissa 09691	12500
5. Use the characteristic “1” before the mantissa to fix the decimal point	12.5

Depending on the notation form/style of the entries (especially the antilog entries) in a traditional table each look-up step in more complex calculations could well have required extra interim interpolation steps to determine the logarithm of each number and the antilog of the resulting mantissa.

Using the graphic logarithmic table by: Lacroix and Ragot

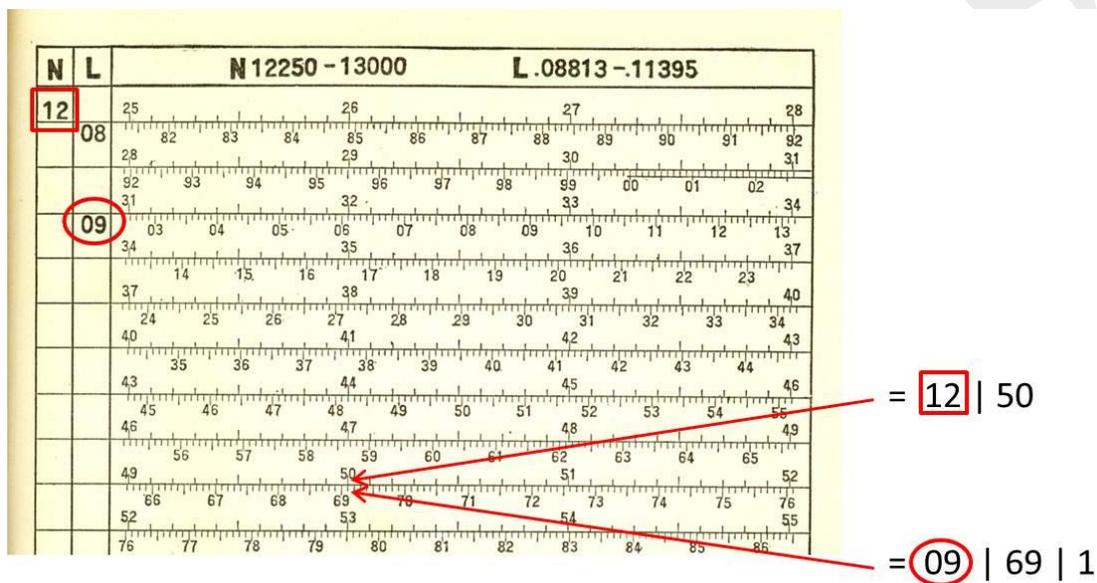
Opting for the longer 40-page table for five decimal places in the book by *Lacroix and Ragot* (see *Appendix A* for the details) the logarithm of 2.5 can be quickly and easily found.



⁶ Half of all the traditional logarithm tables ever published were versions for 4 or 5 decimal places.

Ignoring the decimal point and looking up the leading “25” digits in the “N” column is enough to find the right page in the table. In the adjacent column “L” the leading digits of the logarithm, “39”, are shown. The next step is to locate the following two “00” digits of the number on the upper scale of graduations for log section “39” of the table. The 3rd and 4th digits, “79”, of the logarithm can be found on the lower scale to the left of the tick mark “00”. Finally counting the extra divisions/tick marks that come after 79 before lining up with 00 on the upper scale, gives the last digit of the logarithm: “4”. So, the complete readout is 39 || 79 || 4 or $\log 2.5 = 0.39794$.

The logarithm of “5” can be found equally easily. Adding the two logs (39794 and 69897) gives the same 1.09691 interim answer. But as the log and antilog entries are combined in a graphic logarithmic table, the antilog of the mantissa, “09691”, can be quickly and easily “reverse engineered” using the same intuitive process.



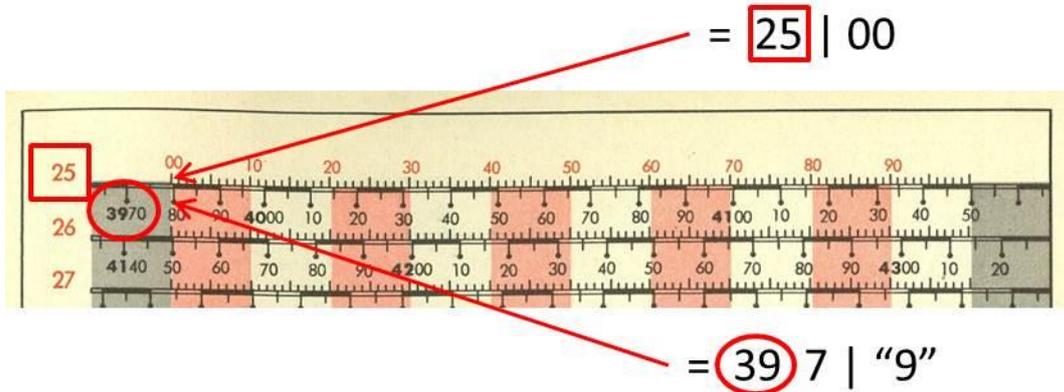
This time looking-up leading “09” digits of the mantissa in column “L” are enough to find the right page in the table and from the column alongside, read off the leading digits of the answer: “12”. Having found the next two digits, “69”, in the log “09” section, one tick mark further for the trailing “1” in the mantissa and the corresponding last two digits of the antilog number can be read off the upper scale – i.e. “50”. After concatenating the two parts and the using the characteristic of the mantissa to fix the decimal point, **12.5** is the answer.

Superficially the steps look similar to using a traditional table of logarithms. However, the graphic version, with its fewer pages and combined log and antilog entries, is certainly less error-prone and much more intuitive to use. Also although both types of tables are compiled for five decimal places, only the graphic version has the inherent potential for accuracy to six decimal places. The values in the worked example finish exactly on a “tick mark” in the scales. But when needed and much like using a slide rule, accuracy to a sixth decimal place by interpolating between two tick marks would be simple and easy to achieve with this table.

Using the graphic logarithmic table by: Koch and Putsbach

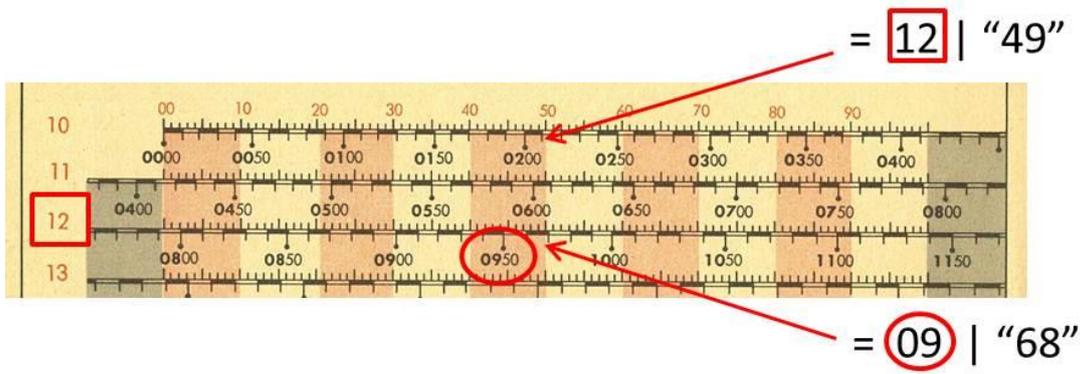
By contrast the table by Koch and Pulsch (see Appendix A for the details) needs interpolation to achieve accuracy to four decimal places. But strikingly the table is

just 4 pages long – highlighting the compactness possible with graphic logarithmic tables compiled for a limited number of decimal places. Needless to say the logarithm of 2.5 can be just as easily found with this version.



Ignoring the decimal point, the leading “25” digits of the number is found in the 1st column on the 2nd page of the table. The next step is again to find the following two “00” digits of the number on the upper scale of graduations for line 25. The corresponding logarithmic value for “00” on the upper scale is between “3970” and “3980” on the lower scale – in fact nearly but not quite “3980”. Using interpolation for the 4th digit, the full readout is 397 || 9 or with this table $\log 2.5 = 0.3979$.

Again the logarithm of “5” can be found equally easily. Although this time, the interim answer after adding the two logs (“3979” and “6989”) is not unsurprisingly slightly less accurate: **1.0968**. As with all such graphic logarithmic tables, the antilog of the mantissa can be just as quickly “reverse engineered” using the same intuitive process already described.



Again the leading “09” digits of the mantissa are used to find the right page in the table and to read off the leading digits of the answer: “12”. The “0968” mantissa lies between two “tick marks”: “0950” and “1000”. Using interpolation to fix “0968” on the scale, the corresponding last two digits of the antilog number can be read off the scale at the top of the page – i.e. “49”. The characteristic of the mantissa again gives the final answer but this time the cumulative effect of working to fewer decimal places means the answer comes out as less precise: **12.49**.

Graphic logarithmic tables – no panacea

Given my opening “A Picture Should Be Worth A Million Numbers” gambit, graphic logarithmic tables should surely have superseded the tedious use of traditional

logarithmic tables. They did not. Instead graphic logarithmic tables are largely unknown and rare.

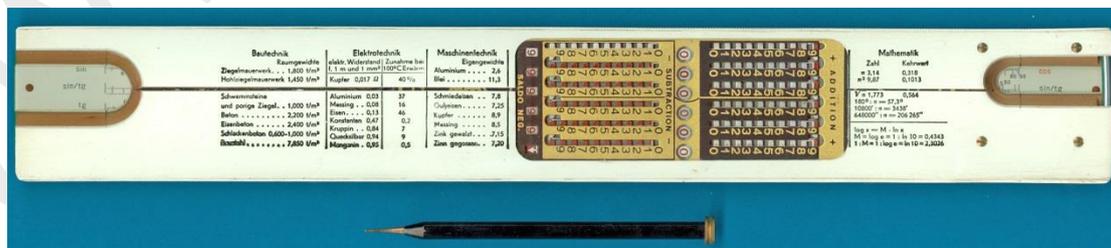
This could be because schools and educational institutions of the day preferred to stick largely to using conventional (and cheaper) mass-produced books of traditional logarithmic tables. But the more probable explanation is that most examples of graphic logarithmic tables are early 20th century developments and some telling inherent limitations meant **they were outdated almost as soon as they were published.**

But who were the intended users of graphic logarithmic tables? Clues can be found in the “*Introductions*” of the more well-known graphic logarithmic tables such as *Pressler, Lacroix and Ragot* and *Leder*. The advantages commonly quoted are speed and size. Reducing the labour-intensive and error-prone process of using a traditional logarithmic table would have obviously appealed to many professions and trades. Condensing the hundreds of pages of a traditional logarithmic table down to a slim volume would also have been preferable to carrying around a bulky book. A modern-day analogy is how the slim *iPad* is commonly preferred to a bulky laptop computer. Ernst Leder goes on to suggest that graphic logarithmic tables could also be: “*a good tool for further education.*” However, early 20th century students who could have been attracted by the advantages of a graphic logarithmic table would almost certainly have opted instead for one of the superior aids of the day – such as the slide rule. Therefore it is even more surprising that a renowned German slide rule maker decided that selected slide rules models would be sold with a graphic logarithmic table!

“*Selling fridges to Eskimos*”

Apart from sharing logarithmic roots, slide rules and graphic logarithmic tables have little in common. They are competing rather than complementary calculating aids. However, German Carl Kübler (1875-1953) must have been a great salesman.

In 1940 Faber-Castell (F-C) decided to supplement their existing portfolio of slide rules with a series of “combination” models. They uniquely were the first to incorporate a mechanical flat sliding bar adder for addition and subtraction into the back of their more popular models. These hybrids became known as their Addiator slide rules⁷ because F-C bought the metal Troncet-type slide adders with an accompanying stylus from *Addiator GmbH*, a company founded by Carl Kübler in 1920. This made good commercial sense as the company was the leading maker of slide adders or Addiators.



What is less clear is how Kübler persuaded F-C they also needed to buy an accompanying 2-page “*Maximator*” paper graphic logarithmic table he had earlier

⁷ Model numbers suffixed by “A” (**A**ddiator) for 25cm and by “R” (**A**ddiator) for pocket 12½cm.

copyrighted. It is illogical but for a brief inexplicable initial two-year period (1940-1942) F-C sold their **1/22A** (Disponent), **1/54A** (Darmstadt) and **1/87A** (Rietz) hybrid models with a “*Maximator*” graphic logarithmic table inserted behind a glued paper strip at the back of the respective instruction booklets (booklet no.’s: 1/702, 1/704 and 1/707). All the booklets included a page on how to use the table.

The *Maximator-Erweiterungs-Tabelle* graphic logarithmic table

After 1942 F-C dropped the “*Maximator*” and opted for a generic instruction booklet for all their Addiator models!

Final paradox

Ironically having started with a *Catch-22* paradox I conclude with another. Early in their evolution compiling and typesetting traditional logarithmic tables was a challenge. Although inherently less error prone, in such times that the graphic printing possibilities were extremely crude and virtually non-existent. By contrast, in the 20th century the possibilities for printing complex images and graphically complex figures were bountiful. This meant graphic logarithmic tables were now relatively easy and economical to publish. However, by the 20th century demands for accuracy had risen sharply. By their very “picture” nature most graphic logarithmic tables, even with the most precise printing or production techniques, only offered 4 or 5 significant places of accuracy. But by now traditional logarithmic tables of 7, 8 or many more significant places had been common place for decades.

Once early 20th century cheaper printing and production techniques became readily available, graphic logarithmic tables could flourish. But sadly by now their level of accuracy had been surpassed and they faced competition from slide rules and other mechanical aids. This meant almost as soon as they became a practical reality, graphic

logarithmic tables **were outdated and inferior**. So unlike the traditional logarithmic table, graphic logarithmic tables (even the often reprinted *Lacroix and Ragot*) **never fulfilled their promise and never became well-known or widely used**.

Acknowledgements & Bibliography

Without the motivating and guiding hand of Klaus Kühn my original research would have been difficult and at best, inconclusive. I am also indebted to Prof. Joachim Fischer for reviewing early on my take on the historical steps associated Napier's development of logarithms.

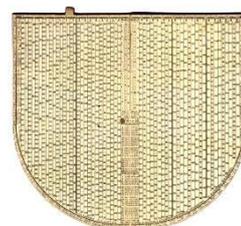
1. **Kühn, Klaus:** "*Collectanea de Logarithmis*", DVD privately produced and distributed by Klaus Kühn, 2013.
2. **Prof. Fischer, Joachim:** "*Napier and the Computation of Logarithms*", JOS Vol. 7 No. 1, Spring 1998, ISSN 1061-6292, 1998, Pg. 11.
3. **Prof. Fischer, Joachim:** "*Looking 'Behind' The Slide Rule: How Did Napier Compute His logarithms?*", Proceedings 3rd Int. Meeting of Slide Rule Collectors, Germany, September 2003, Pg. 8.
4. **Kühn, Klaus:** "*Logarithms – Mini and More*", Proceedings 16th Int. Meeting of Slide Rule Collectors, The Netherlands, September 2010, Pg. 137.
5. **Prof. Fischer, Joachim:** private correspondence, 2010/2011.
6. **Jeziarski, Dieter von:** private correspondence, 2010/2012.
7. **Rudowski, Werner:** loan of examples and private correspondence 2011/2012.
8. **Weiss, Stephan:** "*Steinhäuser's Suggestions for a Slide Rule in 1807*", Proceedings 16th Int. Meeting of Slide Rule Collectors, September 2010, The Netherlands, Pg. 203.
9. **Weiss, Stephan:** "*Ingenieur-Messknecht*", online Great Encyclopedia of Mechanical Calculating - Rechnerlexikon, March 2006.
10. **Irler, Wolfgang J:** "*The Double Use of a Graphical Cardboard Logarithm Table*", Proceedings 18th Int. Meeting of Slide Rule Collectors, September 2012, England, Pg. 126.
11. **Holland, Peter:** "*Printed Logarithmic Calculating Scale by Loewe*", JOS, Vol. 11, No. 1, Spring 2002, ISSN 1061-6292, Pg. 14.
12. **Rance, David:** "*Reckon on it! A very British trait*", Proceedings 15th Int. Meeting of Slide Rule Collectors, September 2009, Germany, Pg. 65.
13. **Chamberlain, Edwin J.:** "*Three American Printed Page Logarithmic Calculating Scales*", JOS Vol. 11 No. 1, Spring 2002, ISSN 1061-6292, Pg. 8.
14. **Diestelkamp, Fredrich:** "*Maximator*", online Great Encyclopedia of Mechanical Calculating - Rechnerlexikon, April 2004.
15. **Joss, Heinz:** "*Maximator-Erweiterungs-Skala*", Rechenschieber-Brief 6, January 2002.
16. **Jeziarski, Dieter von:** "*Faber-Castell-Anleitungen*", RST Newsletter, Rechenschieber-Brief 8, February 2003.
17. **Kordetzky, Hans:** "*Anleitung zum Addiator Universal*", RST-Treffen 24, Bamberg, November 2012.
18. **Rechnerlexikon** "*Carl Kübler*" online encyclopedia of mechanical computing http://www.rechnerlexikon.de/en/artikel/K%FCbler,_Carl .
19. **Holland, Peter:** "*Slide Rules – A.W. Faber & A.W. Faber-Castell*" 7th edition, private publication © 2014.
20. **Venetsianos, Panagiotis,** "*Dr. Haro's New Method of Graphical Notation of Logarithms*", KRING Newsletter, MIR No. 65, May 2014.

Appendix A: Known Graphic Logarithmic Tables

Such tables defy inclusion into any existing classification scheme for similar aids such as Ready Reckoners, Tabular Calculators, etc. So in this compendium (others may well exist) of all the known commercially printed examples⁸ are listed, with a thumbnail image, by the year they were first published.

+/-1852: *Pressler* - Dresden, Germany

Title: *Ingenieur-Messknecht*



By: Maximilian Robert Pressler

Type: Slip cased folding set of tables (with built-in clinometer) printed on escutcheon or shield shaped double-sided stiff cardboard

Size: 20.7cm (longest point i.e. from the Chief to the Base) x 22.4cm (widest point i.e. from the Dexter to the Sinister) x 0.4cm

Published by: Unknown

Patents? None found

Style of table(s): Front and side edges: mixture of tables and conversion factors
Back: mainly a four-place graphic table organised in columns

Length(s) of graphic table: $\approx 5.5\text{m}$

Comments: Probably the first graphic logarithmic table ever published. It was mainly intended for use in the field by forestry workers. But Pressler also claimed it was a universal aid for students calling it a “*Mathematical Cinderella*” – possibly a cryptic reference to it being able to do all kinds of mathematical chores. Pressler also wrote a book to accompany his Messknecht. Various editions of the Messknecht and the book exist.

1893: *Loewe* – Bromberg, Germany

Title: *Rechenscalen für numerisches und graphisches Rechnen*



By: Loewe

Type: Hardback book (50 pages) with a brown cover

Size: 23.3cm x 16.3cm

Published by: Verlag des Technischen Versandgeschäfts R. Reiss⁹

Patents? None found

⁸ As defined in the main part of this paper.

⁹ Nearly two decades later, in 1912, the same Reiss started making slide rules.

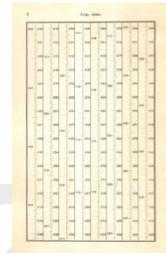
Style of table(s): (i) 5-page four-place graphic table organised in columns
(ii) Three other tables for trigonometrical functions

Length(s) of graphic table: ≈ 10.4 metres

Comments: Interestingly Loewe also includes “*how to calculate*” instructions for using a pair of dividers.

1897: Tichy – Wien, Austria

Title: *Graphische Logarithmen-Tafeln*



By: Anton Tichy

Type: Hardback book (30 pages) with light fawn cover

Size: 24.5cm x 16.0cm

Published by: Verlag des Oesterr. Ingenieur- und Architekten-Vereines, Wien

Patents? None found

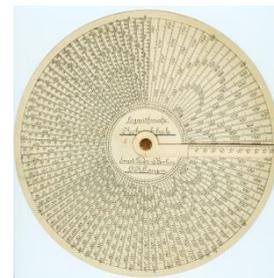
Style of table(s): (i) Four-place graphic table organised in columns
(ii) Other tables for trigonometrical functions

Length(s) of graphic table: ≈ 16 m

Comments: -

1908: Leder - Berlin, Germany

Title: *Die Praxis des Logarithmen-Rechnens*



By: Ernst Leder

Type: Circular cardboard chart with a cardboard cursor as part of a hardback book (125 pages) with pale blue linen cover

Size: Chart: \varnothing 21cm
Book: 27.8cm x 21.9cm

Published by: Verlag der Cito-Rechenmaschinen-Werke G.m.b.H., Berlin

Patents? DE104927 – 15th August 1899
DE223529 – 24th June 1910

Style of table(s): Four-place “graphic table” (antilogs only) organised as radii from the centre of the chart

Length(s) of graphic table: ≈ 6.1 m

Comments: This is the exception to all the other book-style listings. Instead of tables, the entire book consists of advice and worked

examples of how to use logarithms in a myriad of calculations. A sleeve, pasted onto the inside back cover, holds a circular graphic antilogarithm chart. Using the chart as an “antilog table” is explained in the book but the author assumes that the looking-up of logarithms (not possible with the chart) is done with a traditional logarithm table.

1925: Lacroix and Ragot - New York, USA

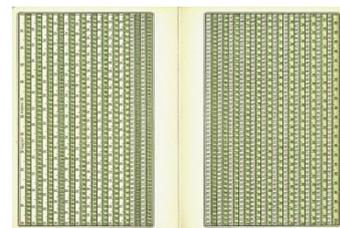
Title: *A Graphic Table combining Logarithms and Anti-Logarithms*



By: Adrien Lacroix and Charles L. Ragot
 Type: Hardback book (52 pages) with green linen cover
 Size: 23.6cm x 15.2cm
 Published by: The Macmillan Company, New York
 Patents? US1610706 – 14th December 1926
 Style of table(s): (i) 40-page five-place without interpolation graphic table organised in rows
 (ii) 6-page four-place graphic table organised in rows
 Length(s) of graphic table: Long version ≈ 115m
 Short version ≈ 13.8m
 Comments: Book reprinted in 1927, 1936, 1938, 1941, 1942 and 1943.

+/-1926: Kübler - Berlin, Germany

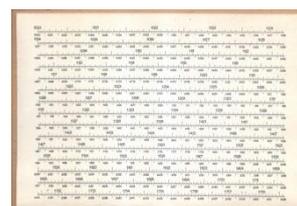
Title: *Maximator Logarithmen Tafel*
Maximator-Erweiterungs-Tabelle



By: Carl Kübler
 Type: Folded card (2 pages)
 Size: 27cm x 18.6cm
 Published by: Addiator GmbH and later A. W. Faber-Castell Vertrieb GmbH
 Patents? None found but design Copyrighted by Addiator GmbH
 Style of table(s): 2-page four place graphic table organised in columns
 Length(s) of graphic table: ≈ 4.1m
 Comments: It was originally sold with the “Maximator” - a desk stand mounted mechanical slide adder from Addiator GmbH. Later included with the early versions (1940-1942) of the Faber-Castell hybrid Addiator models: 1/22A, 1/54A and 1/87A.

1946: Kienbaum - Gummersbach, Germany

Title: *Skalog - Der Skalen-Schnellrechner nach Kienbaum, eine graphische Logarithmentafel*



By: Gerhard Kienbaum¹⁰
Type: Hardback book (12 pages)
Size: 22.4cm x 15.2cm
Published by: Ingenieurbüro Dipl.-Ing. Kienbaum, Gummersbach
Patents? None found
Style of table(s): (i) 4-page four place graphic table organised in rows
(ii) 4-page numeric table for trigonometrical functions
Length(s) of graphic table: $\approx 10.7\text{m}$
Comments: Probably a private publication by Kienbaum.

1949: Rohrberg - Berlin, Germany

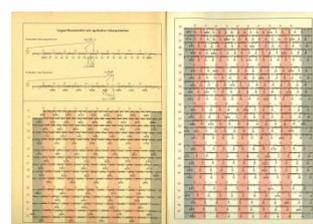
Title: *Graphische Funktionentafeln Graphical Table of Functions Tables Graphiques des Fonctions*



By: Prof. Albert Rohrberg¹¹
Type: Softback book (30 pages) with pale blue cover
Size: 29.9cm x 20.9cm
Published by: Fachverlag Schiele & Schön, Berlin
Patents? None found but copyrighted in 1949
Style of table(s): (i) 7½-page four place graphic table organised in rows
(ii) Four other tables for trigonometrical functions
Length(s) of graphic table: $\approx 11.7\text{m}$
Comments: Multi-language: German, English and French.

1957: Koch and Putschbach - Hannover, Germany

Title: *Schroedels Mathematische und Naturwissenschaftliche Tafeln - Logarithmentafel mit optischer Interpolation*



By: A. Koch and R. Putschbach¹²

¹⁰ Started a one-man business that later became one of Germany's leading consulting companies.

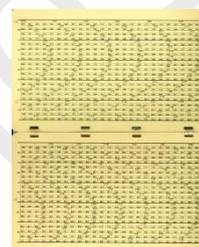
¹¹ Rohrberg also designed Faber-Castell model 342 Columbus "System Rohrberg" specialist slide rule.

¹² Attributed authors of the graphic logarithm table included in the book published by Schroedel.

Type: Hardback book (51 pages) with dark-blue cover
Size: 22.9cm x 16.2cm
Published by: Hermann Schroedel Verlag KG, Berlin, Hannover and Darmstadt
Patents? None found
Style of table(s): (i) Grids of mathematical and scientific constants
(ii) Assorted mathematical tables
(iii) Assorted scientific tables
(iv) 4-page four-place graphic table organised in rows
Length(s) of graphic table: $\approx 11.2\text{m}$
Comments: As a handy “all-in-one” mathematical reference compendium for students it was clearly aimed at schools, etc.

1957: *Obbink* – Den Haag, The Netherlands

Title: *Rekentafel ABACUS Graphische Logaritmentafel*



By: J. B. Obbink
Type: Softback book (36 pages) with a mottled grey cover
Size: 22.5cm x 13.5cm
Published by: Roos en Roos, Arnhem
Patents? None found
Style of table(s): 22-page five-place without interpolation graphic table organised in rows
Length(s) of graphic table: $\approx 88\text{m}$
Comments: Unlike the rest of the book, the graphic log table pages are printed on a much thicker grade/weight of paper. Probably a “private publication” by Obbink.